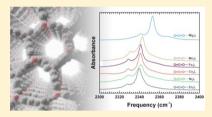


# Insights into the Anomalous Vibrational Frequency Shifts of CO<sub>2</sub> Adsorbed to Metal Sites in Microporous Frameworks

Stephen A. FitzGerald,\*',† Jennifer M. Schloss,†,|| Christopher J. Pierce,† Benjamin Thompson,† Jesse L. C. Rowsell,‡ Kuang Yu,§,\(^{\\$}\) and J. R. Schmidt§

Supporting Information

ABSTRACT: Diffuse reflectance infrared (IR) spectroscopy was used to study the structure and dynamics of H<sub>2</sub> and CO<sub>2</sub> adsorbed within the isostructural metal-organic frameworks  $M_2L$  (M = Mg, Mn, Fe, Co, Zn; L = 2,5-dioxidobenzene-1,4-dicarboxylate) referred to as M-MOF-74 and CPO-27-M. Cluster models of the primary adsorption site were excised from periodic models that were optimized using plane-wave density functional theory at the Perdew-Burke-Ernzerhof (PBE) level. Models incorporating an adsorbed H<sub>2</sub> or CO<sub>2</sub> were optimized using dispersion-corrected density functional theory (DFT), and the anharmonic vibrational frequencies of the adsorbate were



calculated using the discrete variable representation method. The calculated vibrational frequency shifts reveal the same trend among the M<sub>2</sub>L materials as those observed experimentally and provide insight into the origins of these shifts. Our experimental spectra of adsorbed  $CO_2$  confirm a unique blue shift of the  $\nu_3$  mode for molecules adsorbed in  $Mg_2L$ , while the frameworks assembled from transition metals induce a red shift. By shifting the focus to the CO<sub>2</sub> local vibrational modes, a deeper insight into the influence of "back bonding" (metal d-electron density donation into  $CO_2 \pi^*$  orbitals) is revealed; for  $Mg_2L$  there is a nearcomplete cancellation of the opposing local mode contributions to the observed frequency shift. Additional spectral features in the CO<sub>2</sub>  $\nu_3$  region are assigned to (1) the  $\nu_3$  mode of the  $^{13}$ CO<sub>2</sub> isotopologue, (2) a combination mode involving a  $\nu_2$  excitation, and (3) librational sidebands arising from center-of-mass motion of the adsorbed molecule on the surface. Interestingly, below 100 K we observe the appearance of a new band that is distinct from the primary  $\nu_3$  band observed at room temperature. This band is attributed to an alternate, localized orientation of CO<sub>2</sub> adsorbed to the metal site, which is supported by the DFT model.

## ■ INTRODUCTION

Two gases have sustained the attention of environmental and energy science researchers in recent decades: H2 and CO2. From a chemistry standpoint, the former is an ideal energy carrier, being lightweight and producing only water during combustion or oxidative conversion in fuel cells. Dihydrogen is also the simplest molecular species, and its dynamics are the most amenable to accurate modeling by quantum theory. Yet no storage technology has been successfully commercialized to deliver practical quantities of the gas to an automobile motor. 1-3 In the case of CO<sub>2</sub>, much attention has recently been focused on systems for efficient separation of CO2 from gas mixtures, such as those at the heart of contemporary carbon capture and sequestration projects.4-7 In both cases, microporous materials have been proposed as potential materials to overcome these gas storage and separation challenges, with their tremendous surface area yielding high gas uptake via physisorption.

Experimental benchmarks for modeling physisorptive interactions have traditionally been gathered using spectroscopy, wherein the perturbed energies of the translational, rotational, and vibrational quantum states of adsorbed molecules are measured. Infrared (IR) and inelastic neutron scattering (INS)

spectroscopies are the primary techniques that have been employed to study H2 and CO2 adsorbed in microporous materials.<sup>8-17</sup> IR spectroscopy is especially useful because of the smaller capital cost and greater accessibility of the instrumentation, which is easily modified for in situ studies sampling a wide range of temperatures and pressures. 18 In all cases, the connections between spectroscopic observables and molecular structure and dynamics are indirect, often leaving results open to interpretation. Computational results provide an important bridge between experimental observables and the materials properties of interest. When computational results are inconsistent with experimental data, concerns about sample contamination or fundamental shortcomings in the underlying theory must be addressed. It is therefore essential to perform fundamental studies of robust, structurally simple adsorbents using complementary methods to confidently describe adsorption processes for even the smallest of molecules.

Crystalline metal-organic frameworks (MOFs) are ideal materials for fundamental gas adsorption studies. An exemplary

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Department of Physics and Astronomy and Department of Chemistry and Biochemistry, Oberlin College, Oberlin, Ohio 44074,

<sup>§</sup>Theoretical Chemistry Institute and Department of Chemistry, University of Wisconsin—Madison, Madison, Wisconsin 53706, United States

group of such materials is the isostructural series variously referred to as M-MOF-74 or CPO-27-M. 19-21 This hexagonal structure type is assembled from M<sup>II</sup> cations bridged by 2,5dioxidobenzene-1,4-dicarboxylate, and will be referred to herein as M<sub>2</sub>L for brevity. When completely desolvated, the channels of these materials are lined with metals having available coordination sites. This structural attribute has been associated with greater gas uptake under small partial pressure.<sup>22-24</sup> Independent analyses have demonstrated that the Ni<sub>2</sub>L compound exhibits one of the largest (in magnitude) isosteric enthalpies of H<sub>2</sub> adsorption, approaching -13 kJ/mol at small surface coverage. 23-26 Using IR spectroscopy, several of these authors confirmed a distinct correlation between the red shift of the fundamental vibrational mode of H2 and its enthalpy of adsorption at the metal sites.<sup>27</sup> This observation is consistent with the traditional view of the interaction between H2 and metals, involving both  $H_2(\sigma) \to M(nd)$  charge transfer and  $M(nd) \to H_2(\sigma^*)$  "back bonding".<sup>28</sup>

Despite numerous experimental and computational studies of CO<sub>2</sub> adsorbed in the M<sub>2</sub>L series, a detailed picture of the structure and dynamics of this seemingly uncomplicated adsorbate molecule is still emerging. In contrast to H2, it is the Mg<sub>2</sub>L compound that has the largest affinity for CO<sub>2</sub>, with experimental isosteric enthalpies of adsorption reported to be around  $-45~{\rm kJ/mol.}^{29-34}$  IR spectroscopy has been employed to examine the asymmetric mode  $(\nu_3)$  of CO<sub>2</sub> adsorbed by a few members of the M2L series, with independent groups reporting small frequency shifts having no clear correlation with other properties of the materials. 16,17,35,36 There is also a curious difference in the direction of the frequency shifts: Mg2L induces a blue shift of the  $\nu_3$  mode, while the transition metal analogues cause a red shift. The literature contains a variety of explanations for this behavior and a range of discrepant values predicted for the Mg<sub>2</sub>L-induced frequency shift. 16,36,37 X-ray and neutron diffraction studies of Ni<sub>2</sub>L and Mg<sub>2</sub>L have provided compelling evidence for preferential adsorption of  ${\rm CO_2}$  to the available metal coordination sites, in a similar manner as  ${\rm H_2}^{.34,35,38,39}$  To gain further insight about the localized interaction of CO<sub>2</sub> with the Mg sites, <sup>13</sup>C nuclear magnetic resonance (NMR) spectroscopy was recently used to study the rotational motion of the adsorbate. 40 A reinterpretation of the thermal evolution of the spectra was later presented, and was supported by Monte Carlo simulations of the adsorbed CO<sub>2</sub>.<sup>41</sup>

This report describes our collaborative effort to correctly assign the infrared spectroscopic features of  $H_2$  and  $CO_2$  adsorbed in the system of  $M_2L$  materials using insight provided by computational models. We find these models successfully calculate the same trends in vibrational frequency shifts observed in the experimental spectra, despite the contrasting behavior of the two adsorbate molecules. Importantly, we find that the seemingly anomalous spectroscopic signature of adsorbed  $CO_2$  becomes straightforward when examined via a "local mode" perspective, thus providing clear physical insight into the nature of the metal— $CO_2$  interaction.

## PROCEDURE

Samples of the microporous  $M_2L$  adsorbents were prepared and characterized as described in a previous publication. After desolvation, all sample manipulations were performed under air-free conditions in an argon glovebox to prevent the adsorption of water or other coordinating species.

Infrared spectra were acquired using a Bomem DA3 Michelson interferometer equipped with quartz halogen and globar sources, a CaF2 beamsplitter, and a liquid nitrogen cooled mercury cadmium telluride detector. A custom-built diffuse reflectance system with a sample chamber that allows both the temperature and atmosphere of the material to be controlled was utilized for all experiments. 18 Samples of M2L (~10 mg) were transferred under inert atmosphere to a sample cell affixed to a copper slab providing thermal contact to a coldfinger cryostat (Janis ST-300T). Prior to the introduction of CO<sub>2</sub> gas (purity >99.5%), samples were evacuated for several hours at room temperature (294 K). Dosing was achieved at room temperature by loading a calibrated volume to a desired pressure of CO<sub>2</sub>, measured using an Omega PX-303 pressure transducer, and then exposing this gas to the sample cell. The pressure decrease was used to determine the adsorbed concentration of CO<sub>2</sub>. Control runs were performed with He gas to evaluate dead-volume corrections. For spectra obtained below room temperature, no further gas was added to the system, but the pressure was monitored to determine if any additional adsorption occurred. The temperature was maintained with a Lake Shore 331 controller and monitored with a silicon diode thermometer mounted by the sample.

In silico models of the crystalline adsorbents were constructed using the reported atomic coordinates of the solvent-free framework determined by single-crystal X-ray diffraction,<sup>20</sup> and then optimized for each metal using planewave density functional theory at the Perdew-Burke-Ernzerhof (PBE) level with the Vienna Ab initio Simulation Package. 42-45 The calculations employed a 520 eV cutoff, with core electrons treated with the projector augmented wave (PAW) approach and structures converged to within 10 meV/ Å. Finite cluster models containing three metals and bridging organic fragments were excised from each of the periodic models to higher-level treatments of the adsorbate-framework interactions. The size convergence of the cluster models was examined by comparing their results with periodic plane-wave calculations. At a lower yet consistent level of theory (PBE), the computed frequency shifts using both methods agree within 4% for H<sub>2</sub> and 1% for CO<sub>2</sub>, validating the fidelity of our truncation method used in the cluster model. After inserting a H<sub>2</sub> or CO<sub>2</sub> at the primary adsorption site identified by diffraction studies, 35,46 geometry optimizations were conducted using density functional theory (DFT) incorporating Grimme's D2 dispersion correction.<sup>47</sup> In each case, the atomic positions of the adsorbate molecule, the central metal, and the five oxygens bonded to this metal were relaxed while the positions of the other atoms remained fixed. The maximum components of all forces were converged within 1 meV/Å. An Ahlrichs def2-TZVP basis set was used for the central metal atom and adsorbate molecule, while a smaller def2-SVP basis set was used for the other atoms. Following prior work, 24,48 and consistent with the spin states of similar coordination compounds having O-donor ligands, we adopted high-spin configurations for Mn, Fe, Co, and Ni. Additionally, we implemented ferromagnetic spin configurations where appropriate, since our previous work on the Cr3+-containing framework MIL-101 indicated this configuration is slightly lower in energy.<sup>49</sup> The anharmonic vibrational frequencies were computed using the discrete variable representation (DVR) method. In all cases, we observed that the intramolecular potential energy surface (PES) of the adsorbate is best described by PBE0, prompting the use of a "hybrid" approach, as described below. Specifically, geometry optimization at the B3LYP-D (H<sub>2</sub>) or PBE0-D (CO<sub>2</sub>) level was followed by normal-mode analysis. The choice of B3LYP-D for H<sub>2</sub> was motivated by the functional's accurate reproduction of the M···H<sub>2</sub> bond distance as compared to higher-level wave function approaches (vide infra). Subsequent one-dimensional scans were performed along the computed normal mode coordinate at the PBE0-D level, at which point a DVR analysis was performed to compute the anharmonic frequency. This hybrid approach accounts for potential displacement of the B3LYP versus PBE0 minima along the normal mode coordinates, and fully accounts for the diagonal anharmonicity while neglecting any off-diagonal anharmonicity. Further details of the cluster models and additional validation data are provided in the Supporting Information.

## ■ RESULTS AND DISCUSSION

We began by benchmarking our computational methods with the diffuse reflectance IR spectra of  $H_2$  adsorbed in six  $M_2L$  materials (M = Mg, Mn, Fe, Co, Ni, Zn). At low temperature and pressure the fundamental vibrational mode of para- $H_2$ , denoted Q(0), can be confidently assigned for molecules bound to the available metal coordination sites in each material. A comparison of the experimentally measured frequency shifts of the  $H_2$  Q(0) mode with those calculated using our DFT approach is presented in Table 1. The same trend is noted in

Table 1. Comparison of Experimental and Theoretical Quantities for H<sub>2</sub> Adsorbed at the Metal Site in M<sub>2</sub>L Materials<sup>a</sup>

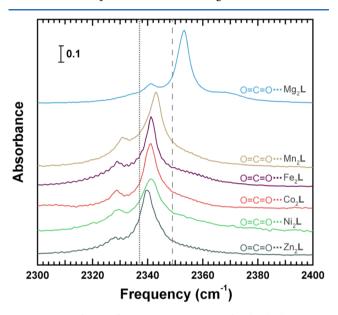
M	$\Delta  u_{ m expt}^{b} ({ m cm}^{-1})$	$\Delta  u_{ m theo}~({ m cm}^{-1})$	$d_{\text{M} \cdot \cdot \cdot \text{H}_2, \text{expt}}$ (Å)	$d_{\text{M}\cdots\text{H}_2,\text{theo}}$ (Å)
Mg	-69	-71	2.45 <sup>c</sup>	2.41
Mn	-73	-83	n/a	2.62
Fe	-100	-96	$2.47^{d}$	2.53
Co	-114	-104	n/a	2.51
Ni	-125	-139	$2.20^{e}$	2.13
Zn	-65	-69	2.6 <sup>f</sup>	2.57

 $^a\Delta\nu$  is the frequency shift of the fundamental vibration Q(0), and  $d_{\text{M...H.}}$  is the distance between the metal and the center of mass of the adsorbed H<sub>2</sub>.  $^b$ Data from refs 26 and 27.  $^c$ Reference 52.  $^d$ Reference 53.  $^c$ Reference 54.  $^f$ Reference 46.

both cases. This trend parallels the Irving—Williams series, as was previously noted for the isosteric enthalpies of  $\rm H_2$  adsorption (at low surface coverage) for these materials. The correlation between the spectroscopic and thermodynamic results is also shared by the  $\rm M\cdots H_2$  interaction distances determined by neutron diffraction, as summarized in Table 1. Several authors have remarked about the consistency of these distinct experimental data with respect to the Kubas-type bonding mechanism used to describe gas adsorption at the metal sites.  $^{13,23,27,50}$  Our computational models successfully reproduce these trends in frequency shifts and  $\rm M\cdots H_2$  distances.

Our calculated frequency shifts for H<sub>2</sub> are significantly larger than those calculated by Chabal and co-workers using van der Waals DFT,<sup>51</sup> likely due to the sensitivity of the shifts to the M···H<sub>2</sub> distances. Those distances are often poorly described by many pure generalized gradient approximation (GGA) functionals (and even some hybrid functionals), and our use of B3LYP-D was chosen after comparison with higher-level wave function-based calculations.

The vibrational structure of  $CO_2$  is obviously more complex than that of  $H_2$ . There are three fundamental vibration modes to consider: the  $\nu_1$  symmetric stretch which is not IR active, the  $\nu_2$  bending mode which is doubly degenerate, and the  $\nu_3$  asymmetric stretching mode which is strongly IR active (only the P and R rovibrational branches are observed in the gas phase). Using the same techniques, instrumentation, and materials described in previous investigations of adsorbed  $H_2$  isotopologues, <sup>26,27</sup> we measured the IR spectra of adsorbed  $CO_2$  at various pressures and temperatures. For this report we focus on the  $\nu_3$  mode, as its frequency appears to be most sensitive to site-specific interactions. Figure 1 shows the IR



**Figure 1.** Diffuse reflectance IR spectra of adsorbed  $CO_2$  in isostructural  $M_2L$  materials at 293 K. The dashed line at 2349 cm<sup>-1</sup> marks the gas phase  $CO_2$   $\nu_3$  frequency and the dotted line at 2337 cm<sup>-1</sup> marks the much weaker band involving the  $\nu_3$  transition of  $CO_2$  in the first excited  $\nu_2$  level. Equilibrium pressures measured during acquisition of the spectra (top to bottom) were 0.2, 1.4, 6.4, 1.8, 6.2, and 11 mbar, respectively. All pressures correspond to concentrations of less than 0.02  $CO_2$  per M. Spectra were measured with 1 cm<sup>-1</sup> resolution and are offset for clarity.

absorption bands assigned to the  $\nu_3$  modes of CO<sub>2</sub> adsorbed at the metal site within the isostructural M<sub>2</sub>L materials. Focusing on the most intense band, we confirm the Mg material is unique in displaying a blue shift relative to the gas phase frequency (dashed line in Figure 1), and our spectra are similar to previous reports on a subset of these materials. <sup>16,17,35,36</sup> The strong IR absorbance of CO<sub>2</sub> in Mg<sub>2</sub>L at a relatively small equilibrium pressure is consistent with the significantly enhanced interaction of the molecule with this particular metal.

Working toward an understanding of the origin of the unique IR signature of  $CO_2$  in  $Mg_2L$ , we computed the  $\Delta\nu_3$  frequency shifts using the methods described above for  $H_2$  adsorption. The results of the DVR calculations are listed in Table 2 alongside the experimental values gleaned from Figure 1. Although the frequency shifts are small, the theory correctly predicts the observed trend. The anomalous blue shift observed for  $Mg_2L$  was previously ascribed to asymmetric distortion of the  $CO_2$  molecule upon adsorption, <sup>16</sup> yet our calculations show no obvious differences in binding geometry or orientation among the optimized structures. Unlike  $H_2$ , there is little

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Table 2. Comparison of Experimental and Theoretical Quantities for CO<sub>2</sub> Adsorbed at the Metal Site in M<sub>2</sub>L Materials<sup>a</sup>

M	$(\text{cm}^{-1})$	$(\mathrm{cm}^{-1})^{\Delta u_{3,\mathrm{theo}}}$	$\frac{\Delta\omega_{1, ext{theo}}}{( ext{cm}^{-1})}$	$\frac{\Delta\omega_{2, ext{theo}}}{( ext{cm}^{-1})}$	d <sub>M···OCO,expt</sub> (Å)	$d_{\text{M}\cdots\text{OCO,theo}} \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $	$\Delta H_{ m expt}$ (kJ/mol)	$\frac{E_{ m theo}}{({ m kJ/mol})}$
Mg	4	2	-53	53	2.24-2.39, <sup>b</sup> 2.27 <sup>c</sup>	2.27	$-43.5$ , $^{c}$ $-47$ , $^{e}$ $-42$ , $^{f}$ $-39$ , $^{g}$ $-73$ , $^{h}$ , $-45$ , $^{i}$ $-42.0$	-44
Mn	-6	-5	-45	35	2.51 <sup>c</sup>	2.51	$-31.7$ , $^{c}$ $-31.9$ <sup><math>i</math></sup>	-33
Fe	-8	-5	-43	34	$2.29^{c}$	2.46	$-33.2$ , $^{c}$ $-34.3$ <sup><math>j</math></sup>	-32
Co	-8	-6	-48	38	2.23, <sup>c</sup> 2.261 <sup>c</sup>	2.38	$-33.6$ , $^{c}$ $-37$ , $^{e}$ $-34.5$ <sup><math>j</math></sup>	-34
Ni	-8	-6	-56	44	$2.29^{d}$	2.29	$-38.6$ , $c^{c}$ $-40$ , $d^{d}$ , $-41$ , $e^{c}$ $-39$ , $f^{f}$ $-38.7$	-39
Zn	-9	-6	-46	35	2.43 <sup>c</sup>	2.44	$-26.8$ , $^{c}$ $-30$ , $^{i}$ $-30.6^{j}$	-33

 $^a\Delta\nu_3$  is the frequency shift of the asymmetric stretching (normal) mode,  $\Delta\omega_1$  is the frequency shift of the local vibrational mode of the C–O bond nearest the metal,  $\Delta\omega_2$  is the frequency shift of the local vibrational mode of the C–O bond farthest from the metal,  $d_{\text{M}-OCO}$  is the distance between the metal and the nearest oxygen atom of the adsorbed  $CO_2$ ,  $\Delta H_{\text{expt}}$  is the enthalpy of adsorption (at small surface coverage) determined by isosteric analysis of gas adsorption isotherms or variable-temperature IR spectroscopy, and  $E_{\text{theo}}$  is the calculated energy of adsorption.  $^bD$ ata from ref 39.  $^cR$ eference 34.  $^dR$ eference 35.  $^dR$ eference 29.  $^fR$ eference 30.  $^gR$ eference 31.  $^bR$ eference 32.  $^fR$ eference 33.

correlation of the  $\mathrm{CO}_2$  frequency shifts with the M···adsorbate distances or adsorption enthalpies, but the optimized structures match the experimental geometries quite well, with the exception of M = Fe (see Table 2). Our calculated geometries do not display the bending distortions of  $\mathrm{CO}_2$  that were originally reported from diffraction models,  $^{35,38,39}_{35,38,39}$  in agreement with a more recent study that concluded these distortions to be artifacts of the  $\mathrm{CO}_2$  orientation disorder.  $^{34}$ 

A more transparent explanation for the IR signature of CO<sub>2</sub> in these model compounds arises when the vibrations are examined from a local mode perspective. In this view, the focus is on the individual C–O bond vibrations, which give rise to the symmetric and asymmetric normal modes through strong vibrational coupling. The normal mode and local mode coordinates are two equivalent basis sets to construct the molecular vibrational Hamiltonian, and the transformation between these two basis sets can be performed using the FG decomposition formalism (see, for example, ref 56). Within this formalism, we decomposed the symmetric and asymmetric normal modes of our computed models into two local C-O stretching modes (i.e., bond vibrations), within the harmonic approximation, yielding a vibrational Hamiltonian in a local mode basis. The calculated harmonic frequencies are essentially identical to their anharmonic counterparts calculated via DVR as described above, validating this additional approximation. As might be expected, the coupling is large (~450 cm<sup>-1</sup>) but essentially constant among the six materials. This coupling gives rise to the usual symmetric and asymmetric normal modes (of which the latter is the experimental observable in this case). Here we focus on the constituent local modes (C-O bond vibrations), which demonstrate more significant frequency shifts and serve as more direct probes of the metal-CO<sub>2</sub> interaction. As shown in Table 2, the local mode of the C2-O1 bond, which is closer to the metal atom, exhibits a strong red shift in all cases  $(\Delta \omega_1)$ , while the local mode of C2–O3 is blueshifted  $(\Delta \omega_2)$ . This is consistent with the interaction of the CO<sub>2</sub> quadrupole moment with the electric field of a point charge. Polarization and charge transfer may further weaken the C2-O1 bond due to its proximity to the metal center. As mentioned above, the coupling between the two CO2 local modes is approximately the same in all of the materials. As such, the small frequency shift of the  $\nu_3$  asymmetric stretch can be interpreted as arising from the opposition between the redand blue-shifted local modes, which yield only small residual frequency shifts when these modes couple to form the resulting normal modes (given by the eigenvalue of the vibrational Hamiltonian). In contrast to the transition-metal-containing

materials, these two shifts are comparable in size for  $CO_2$  in  $Mg_2L$ . We attribute this behavior to an absence of d valence electrons at the Mg site, which precludes "back bonding" (electron density donation into  $CO_2$   $\pi^*$  orbitals). Such an interaction is expected to additionally red shift both local modes approximately equally, yielding a net red shift of the asymmetric stretch.

The conclusions drawn from the local mode analysis are supported by natural bond orbital (NBO) calculations. An isolated gas-phase CO<sub>2</sub> can be described as a resonance hybrid, with double-double, single-triple, and triple-single bond character within the three dominant Lewis structures. In contrast, NBO analysis<sup>57</sup> of the adsorbed CO<sub>2</sub> shows that the single (C2-O1)-triple (C2-O3) resonance structure dominates, likely due to polarization effects. This deviation matches the trends of the computed local frequency shifts, with a red shift of the C2-O1 local mode and a blue shift of the C2-O3 mode. The exception is CO<sub>2</sub> in Fe<sub>2</sub>L, which displays dominant double-double bonding configuration, consistent with its smaller CO<sub>2</sub> local mode shifts. Among the other metals, the magnitudes of the blue C2-O3 frequency shifts are anticorrelated with the non-Lewis antibonding  $(\pi^* + \sigma^*)$ occupancies of the C2–O3 bonds (see Supporting Information, Figure S1), consistent with the idea that the local mode frequency shifts are directly related to interactions which modulate the bonding character of the C-O bonds. The C2-O3 bond in the Mg<sub>2</sub>L case has the smallest antibonding occupancy (due to the missing back-bonding interaction) and thus the largest local blue shift.

Overall, this theoretical approach provides good agreement with the experimental  $\Delta\nu_3$  values shown in Table 2. The model correctly predicts a unique blue shift for CO<sub>2</sub> in Mg<sub>2</sub>L and red shifts when this molecule interacts with transition metal sites. All of the calculated frequency shifts are within a few wavenumbers of the experimental results. For comparison, previous theoretical calculations have shown a large range in values for  $\Delta\nu_3$  (10–15 cm $^{-1}$  blue,  $^{36}$  6–17 cm $^{-1}$  blue,  $^{37}$  0.5 cm $^{-1}$  red $^{16}$ ).

The insight provided by the local mode analysis for  $\mathrm{CO}_2$  can be extended to correlations among other observable properties. In contrast with the asymmetric mode frequency shifts, the local mode frequency shifts correlate well with the experimental enthalpies of adsorption and calculated adsorption energies for the transition-metal-containing materials. Again, the unique nature of  $\mathrm{Mg}_2\mathrm{L}$  is highlighted by this comparison. Recent theoretical studies have suggested that one can understand the trends in adsorption energy in terms of a combination of

electrostatic effects (which are maximized for Mg) and crystal-field-type arguments. <sup>33,58,59</sup> In the case of simple diatomic adsorbates (such as H<sub>2</sub>), the local and normal mode pictures are equivalent, and the normal mode (and thus direct spectroscopic observable) trivially correlates with adsorption energies. When dealing with complex polyatomic molecules, however, the local mode perspective may yield a more intuitive explanation of the metal-adsorbate interactions.

We have also assigned the weaker bands in the IR spectra shown in Figure 1. At the low CO<sub>2</sub> concentrations examined, all of the spectra exhibit a much less intense shoulder red-shifted 12 cm<sup>-1</sup> from the primary band. Data for gas phase CO<sub>2</sub> vibrational transitions from the HITRAN database indicate that this shoulder is a combination band in which a molecule in the first excited bending mode  $(\nu_2)$  undergoes a fundamental transition of the asymmetric stretching mode  $(\nu_3)$ .<sup>60</sup> The fact that this shoulder is red-shifted from the primary band by the same frequency for all samples is more consistent with its assignment as a combination mode and not the pure  $\nu_3$ transition of a CO2 adsorbed on a different site, especially at these small pressures. Other workers have attributed this shoulder to a combination transition of the  $\nu_3$  asymmetric stretching mode and the two  $\nu_2$  bending modes whose degeneracy is broken upon adsorption.<sup>16</sup> We conclude that there is no need to invoke a lifting of the  $\nu_2$  degeneracy, as the shoulder has the same shift from the pure  $\nu_3$  transition as observed for gas phase CO<sub>2</sub>.

A closer inspection of the CO<sub>2</sub> IR spectra reveals the presence of broad sidebands in addition to the sharper features. A spectrum acquired with the Mg material was deconvoluted into five Lorentzian curves (see Figure 2, where a wider frequency range is shown). The three sharp bands are assigned to  $\nu_3$ -based transitions, all blue shifted by comparable amounts from the gas phase frequencies listed in the HITRAN database. In order of decreasing frequency they are the fundamental  $\nu_3$ (2353 cm<sup>-1</sup>), the combination band with  $\nu_2$  (2341 cm<sup>-1</sup>), and the fundamental  $\nu_3$  band of the  $^{13}\text{CO}_2$  isotopologue (2286)

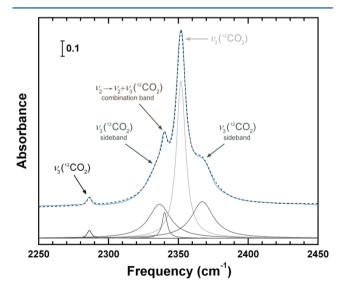


Figure 2. Curve fitting of a spectrum of adsorbed CO<sub>2</sub> in Mg<sub>2</sub>L at 293 K with an equilibrium pressure of 20 mbar, corresponding to a concentration of 0.1 CO<sub>2</sub> per Mg. The solid blue trace is the observed spectrum, and the dotted black trace is the summative fit. Gray traces are the five Lorentzian functions comprising the fit, which have been vertically offset for clarity.

cm<sup>-1</sup>). The fundamental bands of the isotopologues are both shifted from gas phase frequencies by the same 2.8 cm<sup>-1</sup>, while the combination band is shifted by 3.6 cm<sup>-1</sup>. The intensity ratio between the fundamental band and the combination band differs from the ratio listed in HITRAN by a factor of 0.84, which stems from the tendency of the diffuse reflectance method to enhance low-intensity features. The two broader sidebands appear symmetrically shifted by 15.3 cm<sup>-1</sup> to each side of the fundamental band. They were also fit with Lorentzian curves, constrained such that their areas are related by the Boltzmann factor for population of two energy states differing by 15.3 cm<sup>-1</sup>. It is probable that these sidebands correspond to translational or librational transitions occurring with the  $\nu_3$  fundamental transition. This interpretation is consistent with structural models from neutron diffraction studies  $^{38}$  and recent NMR studies which suggest orientational fluctuations of the bound CO2 about its minimum-energy configuration.41

Additional observations related to the dynamics of bound CO<sub>2</sub> are provided by IR spectra collected at lower temperatures. The thermal evolution of spectra acquired from CO<sub>2</sub> adsorbed by Mg<sub>2</sub>L is shown in Figure 3. The gas loading conditions were chosen such that, at room temperature, greater than 95% of the CO<sub>2</sub> molecules in the system are in the adsorbed phase. Since the system is sealed during cooling, we can take the adsorbed concentration to be essentially constant, with at most a 5% increase at the lowest temperature. First, it can be noted that the combination band (2341 cm<sup>-1</sup>) disappears upon cooling, as expected for a band originating from  $CO_2$  in an excited  $(\nu_2)$  vibrational state. Consistent with the findings of Valenzano et al., <sup>36</sup> we do not observe any shift (within 0.1 cm<sup>-1</sup>) in the frequency of the adsorbed species upon cooling to 100 K. This is not surprising, given the very small lattice constant change of Mg<sub>2</sub>L in this temperature range.<sup>39</sup> More striking is the appearance at 75 K of a new band at 2355 cm<sup>-1</sup> that is distinguishable from the fundamental  $\nu_3$ (2353 cm<sup>-1</sup>). The higher frequency band continues to increase in intensity with decreasing temperature at the expense of the other. The two bands also sharpen with cooling, allowing a deconvolution of the spectra into two Lorentzian line shapes. Based on the relative area of these bands, we use a van't Hoff plot (see Supporting Information, Figure S2) to estimate that the enthalpy difference between their configurations is ~1 kJ/ mol. While the lower enthalpy configuration (associated with the 2355 cm<sup>-1</sup> band) is favored at low temperature, the higher enthalpy configuration (associated with the 2353 cm<sup>-1</sup> band) is dominant at higher temperature. Thus, a simple Gibbs free energy consideration,  $\Delta G = \Delta H - T\Delta S$ , shows that this higher enthalpy configuration also has a higher entropy, which our van't Hoff plot puts at ~6 J K<sup>-1</sup> mol<sup>-1</sup>. We hypothesize that each band corresponds to a unique molecular orientation at the primary binding site of the Mg atom. Previous theoretical treatments<sup>61</sup> examining the rotations of an adsorbed CO<sub>2</sub> about a metal center (crudely corresponding to transitions between the two orientations) estimate the energy barrier to be less than 3 kJ/mol, which would allow for interconversion even below 100 K, and thus we can assume the populations of these states are in equilibrium without considering the detailed kinetics of their interconversion. An alternate interpretation of the second band as arising from the occupancy of a secondary site is discounted by a recent NMR study that showed hopping of the  $\mathrm{CO}_2$  between different adsorption sites is frozen out below 150 K.<sup>41</sup>

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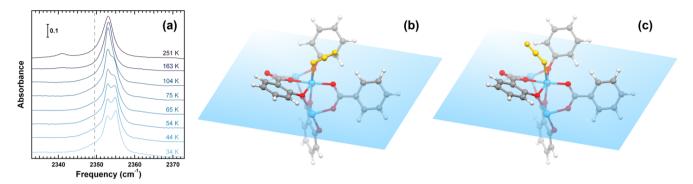


Figure 3. (a) Temperature dependence of the IR spectra of adsorbed  $CO_2$  in  $Mg_2L$  at a concentration of 0.025  $CO_2$  per Mg. The dashed line at 2349 cm<sup>-1</sup> represents the gas phase  $\nu_3$  frequency. (b) Minimum energy orientation of  $CO_2$  (yellow) bound to the adsorption site of a trimetallic cluster model calculated by hybrid DFT methods. (c) Alternate orientation for  $CO_2$  in a local minimum of the same adsorption site. Framework atom colors: C, gray; H, white; Mg, blue; O, red. The blue rectangles represent the mean planes defined by Mg and the four equatorial O atoms in its coordination sphere.

Our DFT calculations confirm the existence of two stable CO<sub>2</sub> adsorption configurations at the primary binding site (see Figure 3). Both involve close approach of a CO<sub>2</sub> oxygen atom with the Mg atom (2.27 Å vs 2.28 Å). The lower energy configuration is more strongly bound due to the shorter distance between the CO<sub>2</sub> carbon and a carboxyl oxygen of the framework (2.75 Å vs 3.07 Å). As such, we predict that the more energetically stable configuration is also lower in entropy, and is thus relatively disfavored at higher temperatures, consistent with dominance of the 2353 cm<sup>-1</sup> band. A harmonic vibrational analysis predicts a larger blue shift for this secondary configuration (5.5 cm<sup>-1</sup> vs 2 cm<sup>-1</sup>), consistent with the experimentally observed frequency difference between the two bands (Figure 3). It should be noted, however, that the calculated energy difference between the two configurations is 8 kJ/mol, larger than the experimental estimate. This may be due to the simplicity of the van't Hoff analysis which assumes that both entropy and enthalpy changes are constant below 100 K. In particular, the large residual conformational freedom of the adsorbed CO2 may generate a nontrivial temperature dependence of the entropy difference between the two configurations.

## CONCLUSIONS

Diffuse reflectance IR spectroscopy provides a detailed probe of the adsorbate-metal interactions in microporous MOFs with coordinatively unsaturated metal sites. We interpret the spectroscopic frequency shifts in terms of perturbations arising from a combination of electrostatics and charge transfer, unique to each metal and adsorbate molecule involved. For polyatomic molecules, the coupling of the adsorbate local modes into normal modes can mask these simple trends, but we find that an intuitive interpretation is restored through a straightforward local mode transformation. For the case of CO2 in Mg2L, our results explain the seemingly anomalous blue shift of the asymmetric  $\nu_3$  mode in terms of the small difference between large and opposing frequency shifts in the two local C-O modes. The size of these calculated local mode shifts is seen to correlate with the binding energy of CO<sub>2</sub> at the metal site. The occurrence of broad sidebands symmetrically shifted from the  $\nu_3$  mode is assigned to librational behavior associated with the rotational degree of freedom of the bound CO2. This orientational freedom is also interpreted as the origin of the two low temperature bands, associated with distinct localminimum-energy configurations.

#### ASSOCIATED CONTENT

## S Supporting Information

Correlation plot from natural bond order analysis, van't Hoff analysis plots, supplementary diagrams of the calculated  ${\rm CO_2}$  orientations at the primary adsorption site, fractional atomic coordinates and unit cell information for calculated periodic models, atomic coordinates of DFT cluster models. This material is available free of charge via the Internet at http://pubs.acs.org.

#### AUTHOR INFORMATION

### **Corresponding Author**

\*E-mail: stephen.fitzgerald@oberlin.edu. Tel.: (440) 775-8334.

## **Present Addresses**

MIT-Harvard Center for Ultracold Atoms, Research Laboratory of Electronics, and Department of Physics, Massachusetts Institute of Technology, Cambridge, MA 02139, USA.

<sup>1</sup>Department of Mechanical and Aerospace Engineering, Princeton University, Princeton, NJ 08533-5263, USA.

#### Notes

The authors declare no competing financial interest.

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